## Area and Volume Homework

Math 1220

In this homework, we will compute some areas and volumes.

Challenge 1. Consider the function $f(x)=\frac{1}{x}$. Find the area of the region bounded by $y=f(x), y=0, x=-e^{2}$, and $x=-e$.

Challenge 2. Let $R$ be the region to the right of $x=1$ bounded above by the curve $y=$ $f(x)=\frac{1}{x}$ and bounded below by $y=0$. Is the area of $R$ finite or infinite? If it is finite, compute the area and if it is infinite, justify your answer.

Challenge 3. Now, take this region $R$ and revolve it around the $x$-axis to create "Gabriel's horn." Compute the volume of Gabriel's horn. (This picture, but solid instead of hollow.)


